

Optimización Introducción Parte III

Enrique E. Tarifa, Facultad de Ingeniería, UNJu

Mapa curricular de la materia

Simulación



Optimización

Mapa curricular de la materia

Simulación

Optimización



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graph TD; A[Simulación] --> B[Optimización]
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Mapa curricular de Optimización

Definiciones

Modelo de optimización

Programación no lineal

Programación lineal

Análisis de sensibilidad



Mapa curricular de Optimización

Definiciones

Modelo de optimización

Programación no lineal

Programación lineal

Análisis de sensibilidad



Mapa curricular de programación no lineal

1. Operación con ciclos
2. Criterio técnico
3. Función objetivo
4. Restricciones
5. Parámetros
6. Variables de decisión
7. Regresión
8. Resolución con LINGO y Excel

Extracción por solvente

Extracción por solvente

Un equipo de extracción con solvente opera con ciclos iguales. La preparación del equipo para cada ciclo demora $t_p = 0.25$ h. La cantidad m (kg) de producto extraído en un tiempo t (h) está dada por la siguiente correlación:

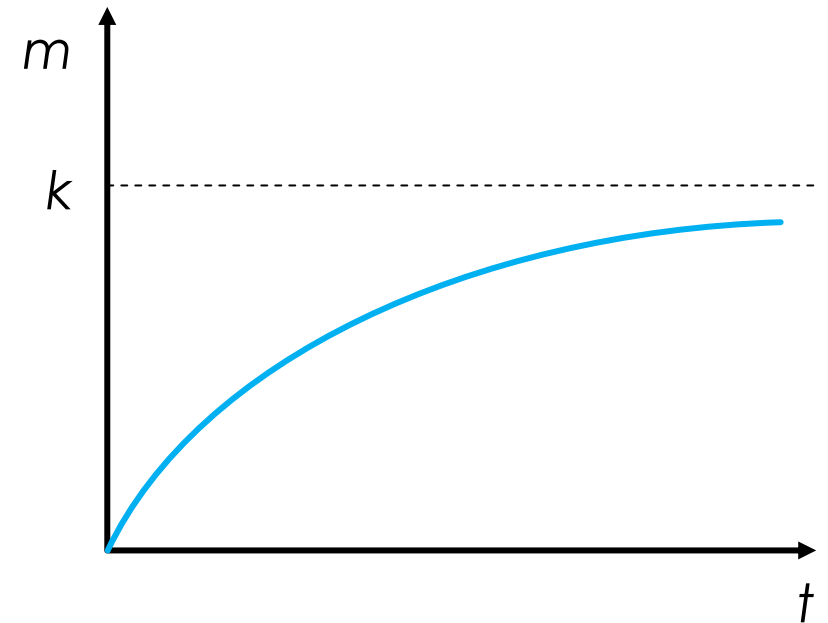
$$m = k(1 - e^{-t/\tau})$$

donde $k = 15$ kg y $\tau = 10$ h.

Se debe extraer $m_o = 150$ kg en el menor tiempo t_o posible.

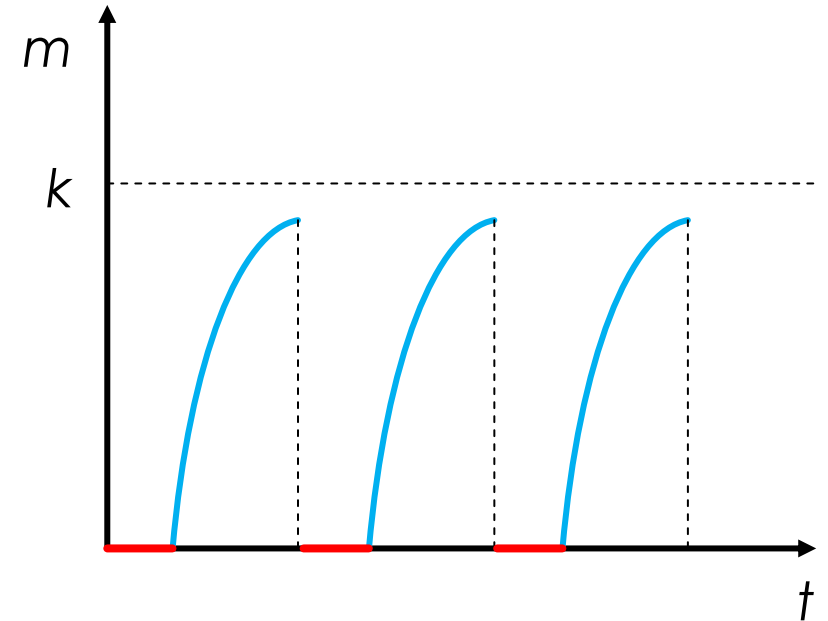
Problema

- En ciclo: $m = k(1 - e^{-t/\tau})$.
- Un $n = 1$ ciclo no es suficiente porque $m_0 > k$.

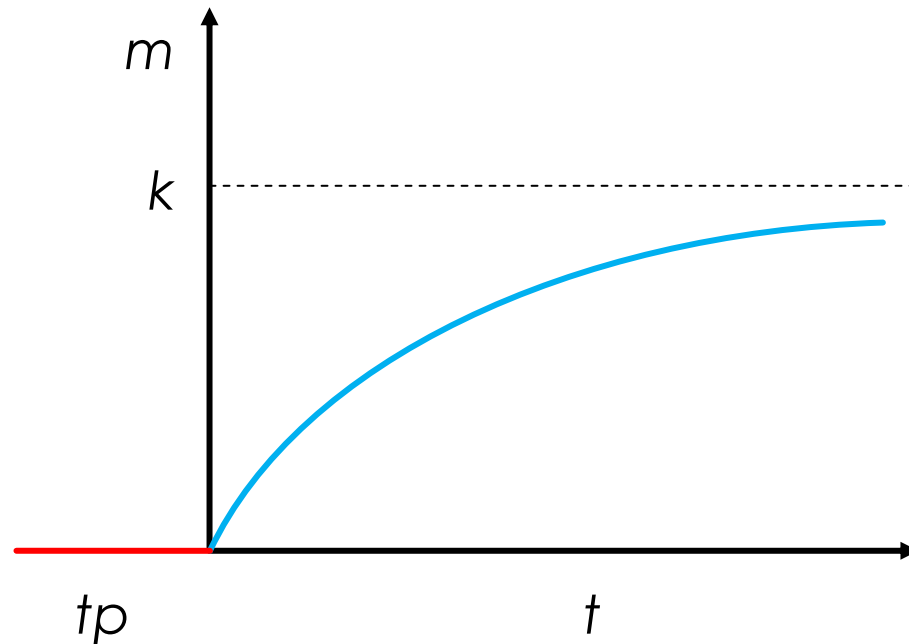


Valores extremos

- Operación con n ciclos.
- Un valor alto de n implica sumar n tiempos muertos.
- Debe haber un valor óptimo de n intermedio.

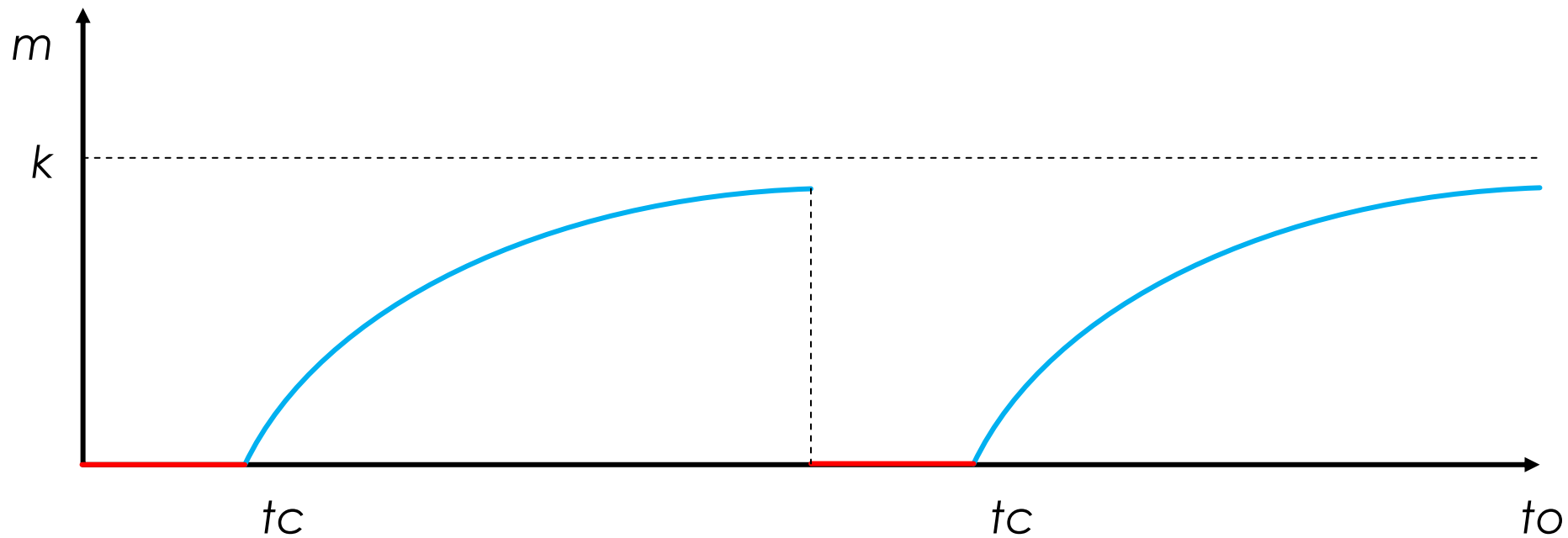


Tiempo de un ciclo



- Tiempo de ciclo (h): $t_c = t_p + t$.
- Extracción por ciclo (kg): $m = k(1 - e^{-t/\tau})$.

Varios ciclos



- Tiempo de operación (h): $to = n tc$.
- Extracción total (kg): $mo = n m$.

Elementos del modelo

- Criterio: Técnico
- Función objetivo:
 - Tiempo de operación (h): t_o .
- Restricciones:
 - Tiempo de ciclo (h): $t_c = t_p + t$.
 - Tiempo de operación (h): $t_o = n t_c$.
 - Extracción total (kg): $m_o = n m$.
 - Extracción de ciclo (kg): $m = k(1 - e^{-t/\tau})$.

Elementos del modelo

Parámetros

- $t_p = 0.25$ h/ciclo
- $k = 15$ kg/ciclo
- $\tau = 10$ h/ciclo
- $m_o = 150$ kg

Variables de decisión

- t_o : Tiempo total de operación (h).
- t_c : Duración del ciclo (h/ciclo).
- t : Duración de la extracción en un ciclo (h/ciclo).
- n : Cantidad de ciclos (ciclo).
- m : Masa extraída en un ciclo (kg/ciclo).

Modelo estándar

$$\text{Min } t_o$$

to,tc,t,n,m

s. a:

$$tc = tp + t$$

$$t_o = n tc$$

$$m_o = n m$$

$$m = k \left(1 - e^{-t/\tau} \right)$$

$$t_o \geq 0, tc \geq 0, t \geq 0$$

$$n \in \mathbb{N}, m \geq 0$$

- $tp = 0.25$ h/ciclo
- $k = 15$ kg/ciclo
- $\tau = 10$ h/ciclo
- $m_o = 150$ kg

$$GL = 5 - 4 = 1 > 0$$

Extracción por solvente.lg4

Modelo en LINGO

- No es necesario despejar variables.
- No es necesario ordenar las restricciones.

```
Lingo Model - Extracción por solvente
! Extracción por solvente;
Data:
  k = 15;      ! kg/ciclo;
  tau = 10;    ! h/ciclo;
  tp = 0.25;  ! h/ciclo;
  mo = 150;   ! kg;
EndData

[FO]  Min = to;

[Rtc] tc = tp+t;
[Rto] to = n*tc;
[RMo] mo = n*m;
[RM]  m = k*(1-@exp(-t/tau));
[Rn]  @gin(n);
```

Resultados en LINGO

Variable	Value	Reduced Cost
K	15.00000	0.000000
TAU	10.00000	0.000000
TP	0.2500000	0.000000
MO	150.0000	0.000000
TO	124.0585	0.000000
TC	2.385741	0.000000
T	2.135741	0.000000
N	52.00000	0.4788611E-02
M	2.884615	0.000000

Row	Slack or Surplus	Dual Price
FO	124.0585	-1.000000
RTC	0.000000	-52.00000
RTO	0.000000	-1.000000
RMO	0.000000	0.8253968
RM	-0.4748330E-07	42.92063

Análisis de la solución

- Valor óptimo $t_c = 2.385741 \text{ h} = 2 \text{ h } 23 \text{ min } 8.67 \text{ s}$
- No es práctico.
- Valor práctico $t_c = 2.25 \text{ h} = 2 \text{ h } 15 \text{ min.}$
- ¿Cuál sería el nuevo procedimiento de operación?

Modificación del modelo

- $GL = 5 - 4 = 1 > 0$
- Al fijar tc , $GL = 4 - 4 = 0$.
- Alternativas:
 - Relajar $mo = n m$.
 - Relajar $n \in \mathbb{N}$.

Min to
 to, tc, t, n, m

s. a:

$$tc = tp + t$$

$$to = n tc$$

$$mo = n m$$

$$m = k \left(1 - e^{-t/\tau} \right)$$

$$to \geq 0, tc \geq 0, t \geq 0$$

$$n \in \mathbb{N}, m \geq 0$$

Alternativa 1

Solución original

- $t_c = 2 \text{ h } 23 \text{ min } 8.67 \text{ s}$
- $m_o = n m$
- $t_o = 124 \text{ h } 3 \text{ min } 30.6 \text{ s}$
- $n = 52 \text{ ciclos}$
- $n m = m_o = 150 \text{ kg}$

Solución alternativa 1

- $t_c = 2 \text{ h } 15 \text{ min}$
- $m_o \leq n m$
- $t_o = 126 \text{ h}$
- $n = 56 \text{ ciclos}$
- $n m = 152.266184 \text{ kg} > m_o = 150 \text{ kg}$

Alternativa 2

Solución original

- $t_c = 2 \text{ h } 23 \text{ min } 8.67 \text{ s}$
- $m_o = n m$
- $t_o = 124 \text{ h } 3 \text{ min } 30.6 \text{ s}$
- $n = 52 \text{ ciclos}$
- $n m = m_o = 150 \text{ kg}$

Solución alternativa 2

- $t_c = 2 \text{ h } 15 \text{ min}$
- $n \geq 0$
- $t_o = 124 \text{ h } 7 \text{ min } 29.28 \text{ s}$
- $n = 55.16656 \text{ ciclos}$
- $n m = m_o = 150 \text{ kg}$
- El último ciclo debe tener una duración menor que t_c .

Regresión

Línea de tendencia

T (K)	σ_{Ge} (10^{-4} S/cm)
400	0.05
500	0.10
600	0.20
700	0.40
800	1.00
900	2.00
1000	4.00



Conductividad Ge - Regresión.xlsx

Regresión lineal

- n : Cantidad de puntos (x_i, y_i) a ajustar.
- $y = ax + b$
- a y b : parámetros a ajustar.

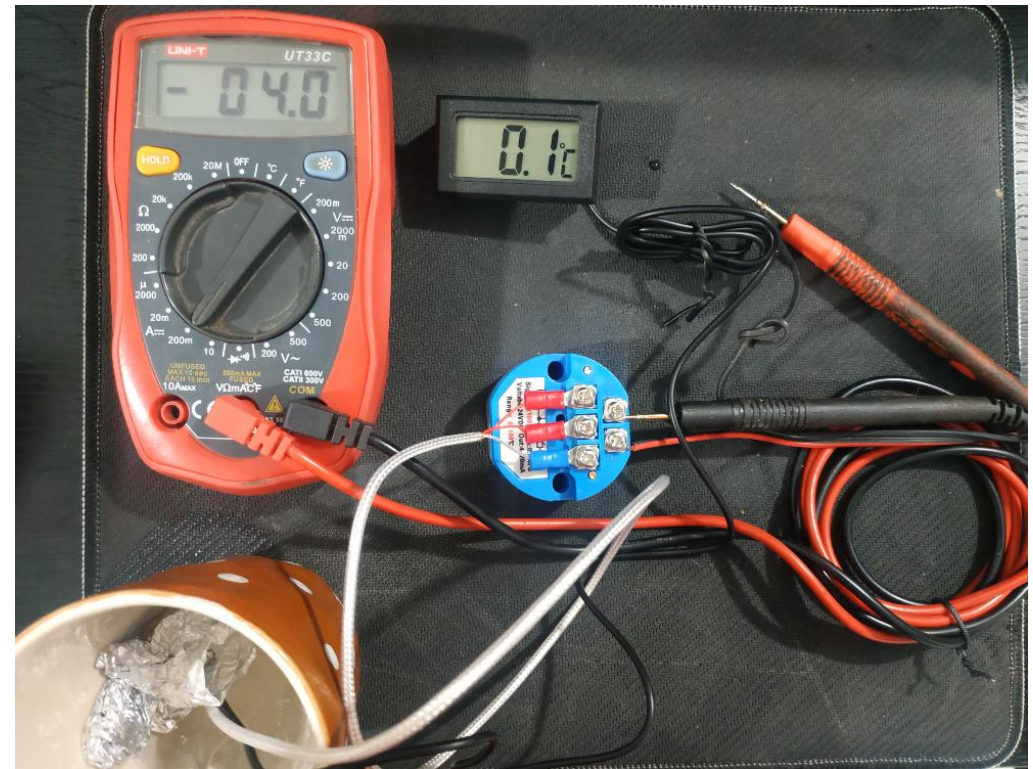
$$\text{Min}_{a,b} \sum_{i=1}^n (y_i - (ax_i + b))^2$$

Regresión lineal

- $Y = \beta_0 + \beta_1 X$
- $S(\beta_0, \beta_1) = \sum_{i=1}^n (y_i - (\beta_0 + \beta_1 x_i))^2$
- $\frac{\partial S}{\partial \beta_0} = 0, \frac{\partial S}{\partial \beta_1} = 0$
- $\hat{\beta}_1 = \frac{\sum_{i=1}^n x_i y_i - n \bar{x} \bar{y}}{\sum_{i=1}^n x_i^2 - \frac{1}{n} (\sum_{i=1}^n x_i)^2}$
- $\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}$
- En Excel:
ESTIMACION.LINEAL(Y,x)

Calibración de un transmisor para una Pt100

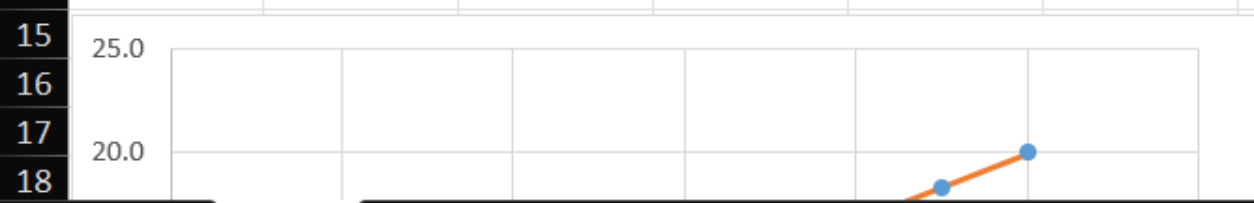
T (°C)	I (mA)
0.4	4.0
10	5.3
20	7.0
30	8.5
40	10.4
50	12.0
60	13.3
70	15.1
80	16.6
90	18.3
100	20.0



	A	B	C	D	E	F	G	H	I	J	K	L	M
1	T (°C)	I (mA)	I(T)	Error²		a	b						
2	0.4	4.0	4	1.78E-02		1.61E-01	3.8019787						
3	10	5.3	5	1.28E-02									
4	20	7.0	7	5.90E-04									
5	30	8.5	9	1.83E-02									
6	40	10.4	10	2.35E-02									
7	50	12.0	12	2.02E-02									
8	60	13.3	13	2.85E-02									
9	70	15.1	15	3.96E-04									
10	80	16.6	17	8.33E-03									
11	90	18.3	18	5.84E-06									
12	100	20.0	20	7.47E-03									
13			Suma =	1.38E-01									

Con la función de Excel.

$$\text{Min}_{a,b} \sum_{i=1}^n (y_i - (ax_i + b))^2$$

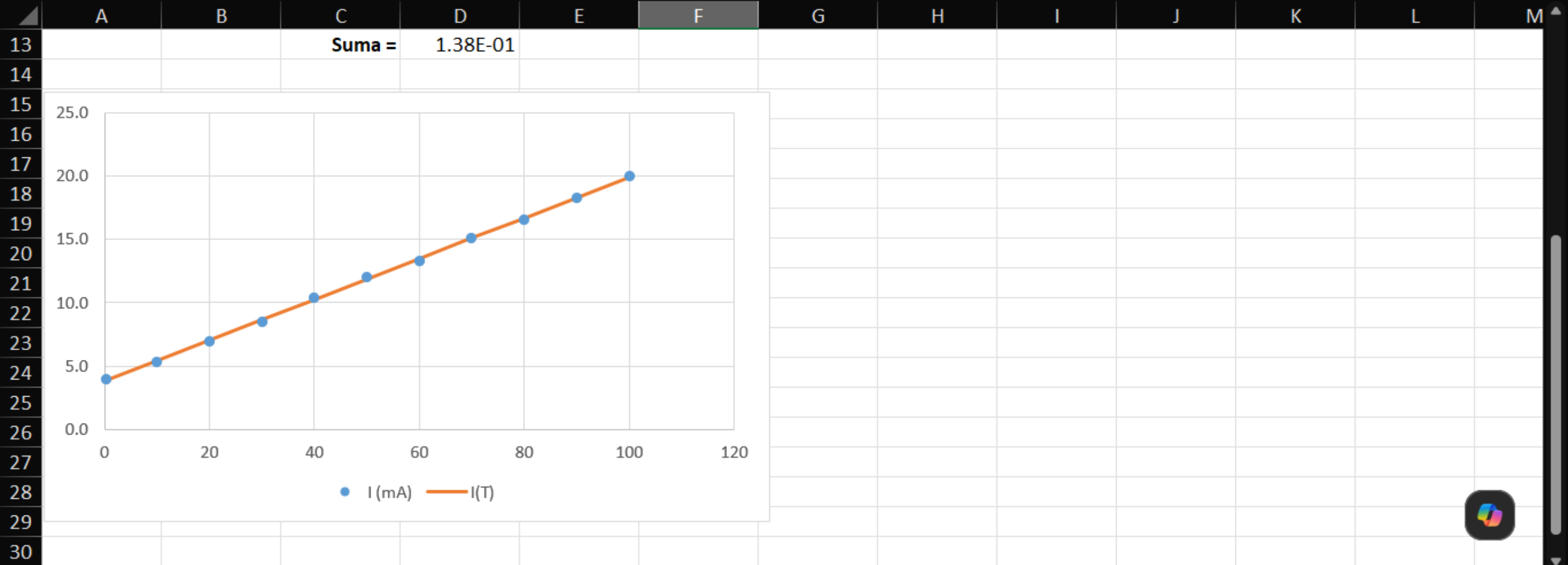


Archivo Inicio Insertar Dibujar Disposición de página Fórmulas Datos Revisar **Vista** Automatizar Programador Ayuda

Predeterminado 📄 Diseño de página 🌙 Cambiar entre modos de 🏠 Mostrar 🔍 Zoom 📄 100% 🔍 Ampliar selección + Nueva ventana 📄 Organizar todo 🔍 Inmovilizar 📄 Cambiar ventanas 📄 Macros

Vista de hoja Vistas de libro Modo oscuro Zoom Ventana Macros

F3 ✖ ✓ f_x



Lineal sol | Lineal | No lineal | No lineal 2 | +

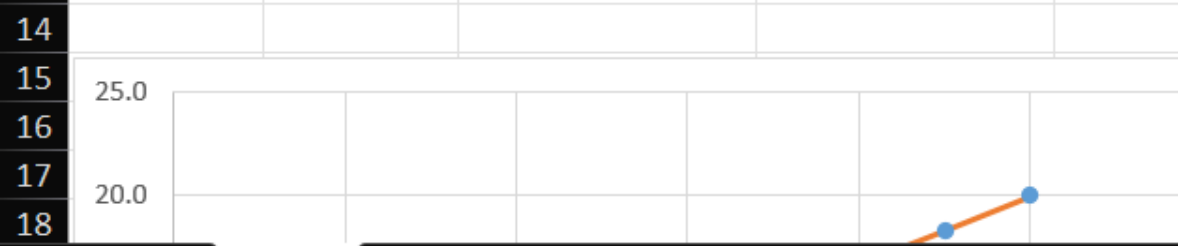
Archivo Inicio Insertar Dibujar Disposición de página Fórmulas Datos Revisar Vista Automatizar Programador Ayuda Comentarios Compartir

Portapapeles Fuente Alineación Número Estilos Celdas Edición Complementos

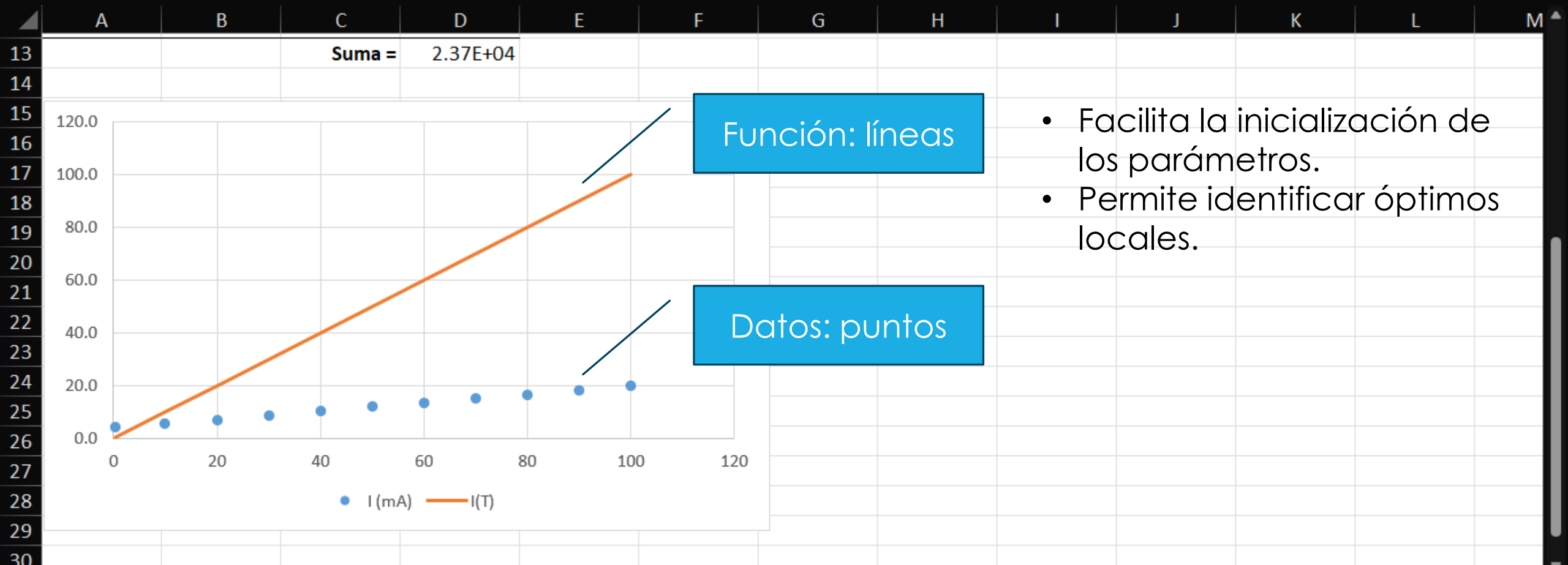
DISTR.T.2C = ESTIMACION.LINEAL(B2:B12,A2:A12)

	A	B	C	D
1	T (°C)	I (mA)	I(T)	Error ²
2	0.4	4	=F\$2*A2+G\$2	=(B2-C2)^2
3	10	5.3	=F\$2*A3+G\$2	=(B3-C3)^2
4	20	7	=F\$2*A4+G\$2	=(B4-C4)^2
5	30	8.5	=F\$2*A5+G\$2	=(B5-C5)^2
6	40	10.4	=F\$2*A6+G\$2	=(B6-C6)^2
7	50	12	=F\$2*A7+G\$2	=(B7-C7)^2
8	60	13.3	=F\$2*A8+G\$2	=(B8-C8)^2
9	70	15.1	=F\$2*A9+G\$2	=(B9-C9)^2
10	80	16.6	=F\$2*A10+G\$2	=(B10-C10)^2
11	90	18.3	=F\$2*A11+G\$2	=(B11-C11)^2
12	100	20	=F\$2*A12+G\$2	=(B12-C12)^2
13			Suma =	=SUMA(D2:D12)

a b
 B12,A2:A12

$$\text{Min}_{a,b} \sum_{i=1}^n (y_i - (ax_i + b))^2$$


Objeto 1 : \times \checkmark f_x =INCRUSTAR("Equation.DSMT4","")



Función: líneas

Datos: puntos

- Facilita la inicialización de los parámetros.
- Permite identificar óptimos locales.

C2 : fx =F\$2*A2+F\$3

	A	B	C	D
1	T (°C)	I (mA)	I(T)	Error ²
2	0.4	4	=F\$2*A2+F\$3	=(B2-C2)^2
3	10	5.3	=F\$2*A3+F\$3	=(B3-C3)^2
4	20	7	=F\$2*A4+F\$3	=(B4-C4)^2
5	30	8.5	=F\$2*A5+F\$3	=(B5-C5)^2
6	40	10.4	=F\$2*A6+F\$3	=(B6-C6)^2
7	50	12	=F\$2*A7+F\$3	=(B7-C7)^2
8	60	13.3	=F\$2*A8+F\$3	=(B8-C8)^2
9	70	15.1	=F\$2*A9+F\$3	=(B9-C9)^2
10	80	16.6	=F\$2*A10+F\$3	=(B10-C10)^2
11	90	18.3	=F\$2*A11+F\$3	=(B11-C11)^2
12	100	20	=F\$2*A12+F\$3	=(B12-C12)^2

a = 1

b = 0

$$\text{Min}_{a,b} \sum_{i=1}^n (y_i - (ax_i + b))^2$$



Obtener y transformar datos Consultas & conexiones Tipos de datos Ordenar Filtro Avanzadas Texto en columnas Esquema Solver

	A	B	C	D	E	F
1	T (°C)	I (mA)	I(T)	Error²		
2	0.4	4.0	0	1.30E+01	a =	1.00E+00
3	10	5.3	10	2.21E+01	b =	0.00E+00
4	20	7.0	20	1.69E+02		
5	30	8.5	30	4.62E+02		
6	40	10.4	40	8.76E+02		
7	50	12.0	50	1.44E+03		
8	60	13.3	60	2.18E+03		
9	70	15.1	70	3.01E+03		
10	80	16.6	80	4.02E+03		
11	90	18.3	90	5.14E+03		
12	100	20.0	100	6.40E+03		
13			Suma =	2.37E+04		

$$\text{Min}_{a,b} \sum_{i=1}^n (y_i - \dots)$$

Parámetros de Solver

Establecer objetivo:

Para: Máx Mín Valor de:

Cambiando las celdas de variables:

Sujeto a las restricciones:

Convertir variables sin restricciones en no negativas

Método de resolución:

Método de resolución
 Seleccione el motor GRG Nonlinear para problemas de Solver no lineales suavizados. Seleccione el motor LP Simplex para problemas de Solver lineales, y seleccione el motor Evolutionary para problemas de Solver no suavizados.

Archivo Inicio Insertar Disposición de página Fórmulas **Datos** Revisar Vista Automatizar Programador Ayuda

Obtener y transformar datos Actualizar todo Consultas y conexiones Consultas & conexiones

Cotizaciones Monedas Tipos de datos

Ordenar Filtro Ordenar y filtrar

Herramientas de datos

Previsión

Análisis

	A	B	C	D	E	F
1	T (°C)	I (mA)	I(T)	Error²		
2	0.4	4.0	4	1.78E-02	a =	1.61E-01
3	10	5.3	5	1.28E-02	b =	3.80E+00
4	20	7.0	7	5.90E-04		
5	30	8.5	9	1.83E-02		
6	40	10.4	10	2.35E-02		
7	50	12.0	12	2.02E-02		
8	60	13.3	13	2.85E-02		
9	70	15.1	15	3.96E-04		
10	80	16.6	17	8.33E-03		
11	90	18.3	18	5.84E-06		
12	100	20.0	20	7.47E-03		
13			Suma =	1.38E-01		

$$\text{Min}_{a,b} \sum_{i=1}^n (y_i - \dots)$$

Resultados de Solver

Solver encontró una solución. Se cumplen todas las restricciones y condiciones óptimas.

Conservar solución de Solver

Restaurar valores originales

Volver al cuadro de diálogo de parámetros de Solver

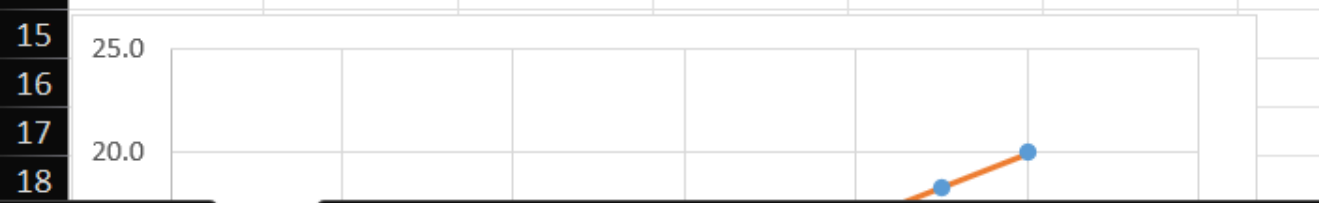
Informes de esquema

Informes: Responder, Sensibilidad, Límites

Aceptar Cancelar Guardar escenario...

Solver encontró una solución. Se cumplen todas las restricciones y condiciones óptimas.

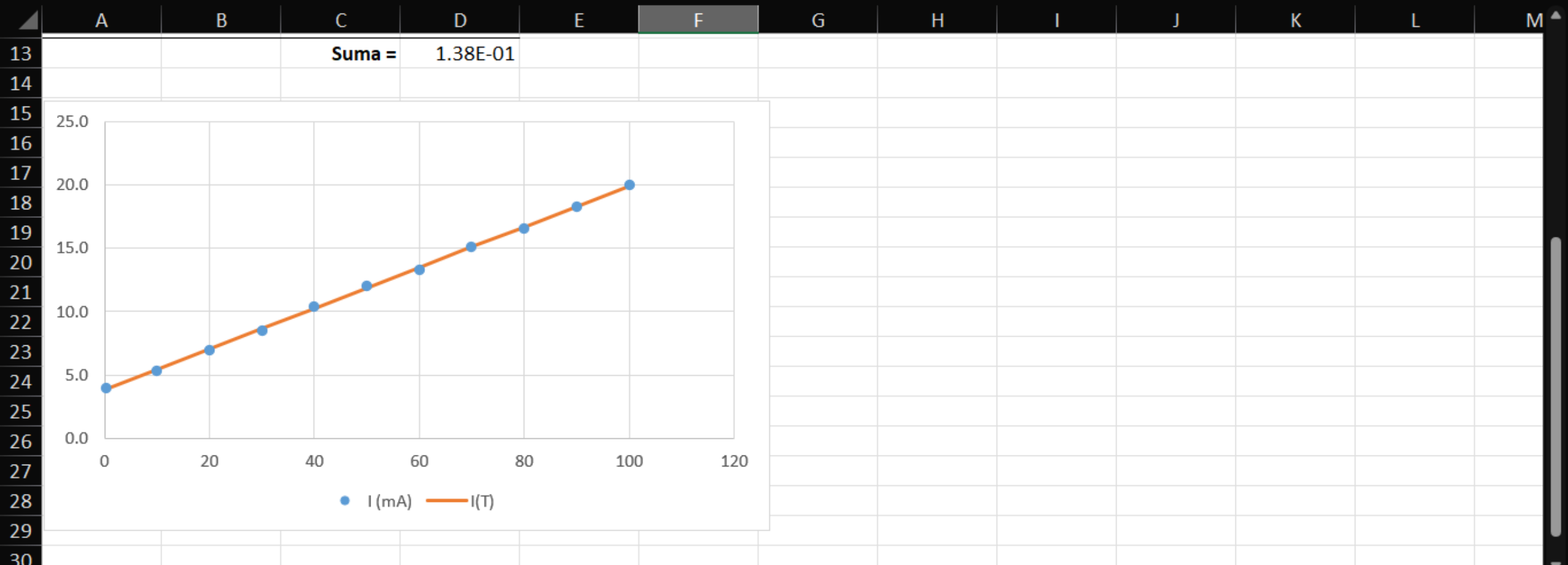
Al usar el motor GRG, Solver ha encontrado al menos una solución óptima local. Al usar Simplex LP, significa que Solver ha encontrado una solución óptima global.



Archivo Inicio Insertar Disposición de página Fórmulas **Datos** Revisar Vista Automatizar Programador Ayuda Comentarios Compartir

Obtener y transformar datos Actualizar todo Consultas y conexiones Consultas & conexiones Tipos de datos Ordenar y filtrar Herramientas de datos Previsión Análisis

F4



Regresión no lineal

- Correlación de Vogel para ajustar la viscosidad del agua de mar.
- $\mu = e^{\frac{a}{T+b}+c}$
- a , b y c : Parámetros a ajustar.

$$\text{Min}_{a,b,c} \sum_{i=1}^n \left(\mu_i - e^{\frac{a}{T_i+b}+c} \right)^2$$

T (C°)	μ (cP)
10	1.30
20	1.00
30	0.80
40	0.65
50	0.54
60	0.46
70	0.40
80	0.35
90	0.31

Regresión.xlsx

	A	B	C	D	E	F	G	H	I	J	K	L
1	T (C°)	μ (cP)	μ(T)	Error²								
2	10	1.30	148.41	2.16E+04	a =	1.00E+02						
3	20	1.00	28.03	7.31E+02	b =	1.00E+01						
4	30	0.80	12.18	1.30E+02	c =	0.00E+00						
5	40	0.65	7.39	4.54E+01								
6	50	0.54	5.29	2.26E+01								
7	60	0.46	4.17	1.38E+01								
8	70	0.40	3.49	9.55E+00								
9	80	0.35	3.04	7.22E+00								
10	90	0.31	2.72	5.80E+00								
11			Suma =	2.26E+04								

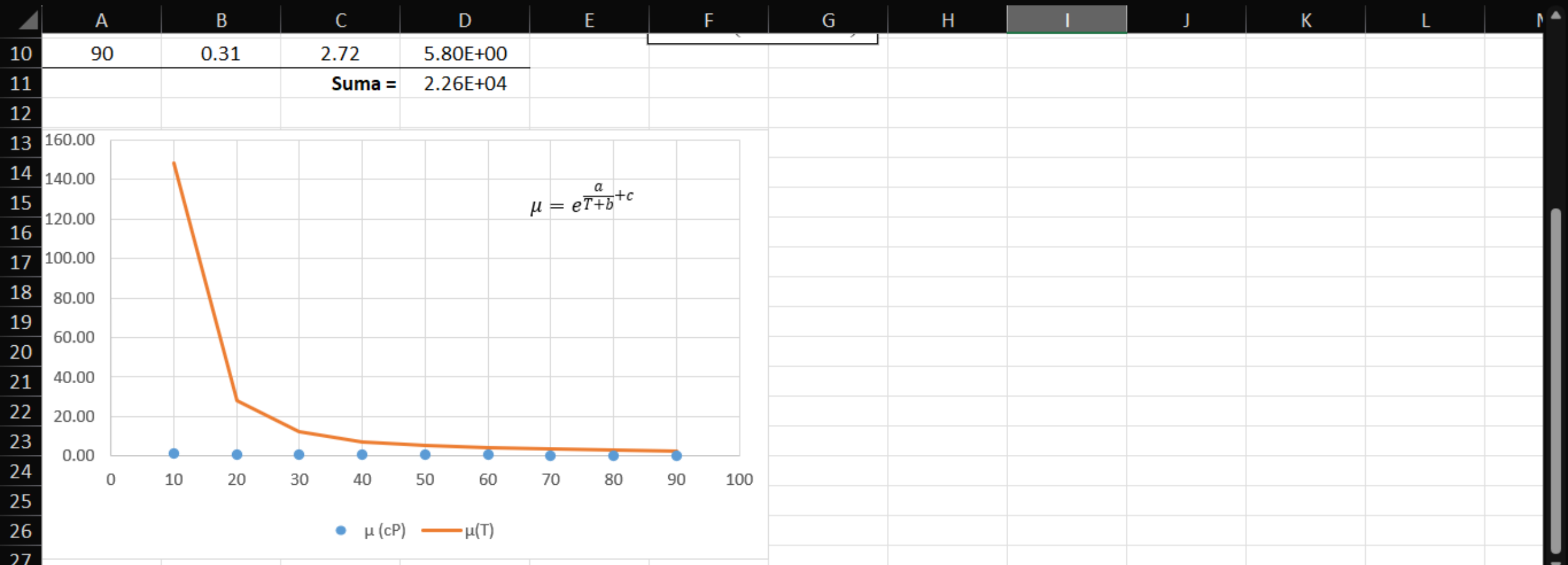
$$\text{Min}_{a,b,c} \sum_{i=1}^n \left(y_i - e^{\frac{a}{T_i+b}+c} \right)^2$$



$$\mu = e^{\frac{a}{T+b}+c}$$

Calibri 11 Fuente Alineación General Formato condicional Insertar Eliminar Formato Edición Complementos Copilot

13 fx



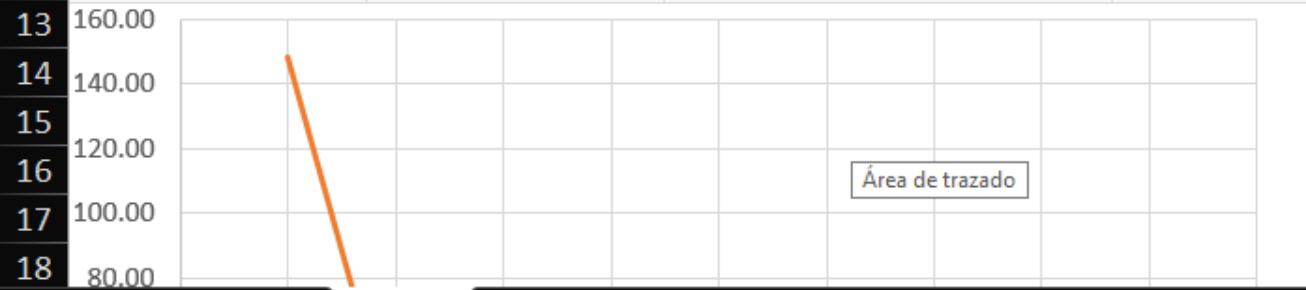
Portapapeles
Calibri 11
N K S
Alineación
Número
Estilos
Celdas
Edición
Complementos

C2 =EXP(F\$2/(A2+F\$3)+F\$4)

	A	B	C	D	E	F	G
1	T (C°)	μ (cP)	μ(T)	Error ²			
2	10	1.3	=EXP(F\$2/(A2+F\$3)+F\$4)	=(B2-C2)^2		a = 100	
3	20	1	=EXP(F\$2/(A3+F\$3)+F\$4)	=(B3-C3)^2		b = 10	
4	30	0.8	=EXP(F\$2/(A4+F\$3)+F\$4)	=(B4-C4)^2		c = 0	
5	40	0.65	=EXP(F\$2/(A5+F\$3)+F\$4)	=(B5-C5)^2			
6	50	0.54	=EXP(F\$2/(A6+F\$3)+F\$4)	=(B6-C6)^2			
7	60	0.46	=EXP(F\$2/(A7+F\$3)+F\$4)	=(B7-C7)^2			
8	70	0.4	=EXP(F\$2/(A8+F\$3)+F\$4)	=(B8-C8)^2			
9	80	0.35	=EXP(F\$2/(A9+F\$3)+F\$4)	=(B9-C9)^2			
10	90	0.31	=EXP(F\$2/(A10+F\$3)+F\$4)	=(B10-C10)^2			
11			Suma =	=SUMA(D2:D10)			

$$\text{Min}_{a,b,c} \sum_{i=1}^n \left(y_i - e^{\frac{a}{T_i+b}+c} \right)^2$$

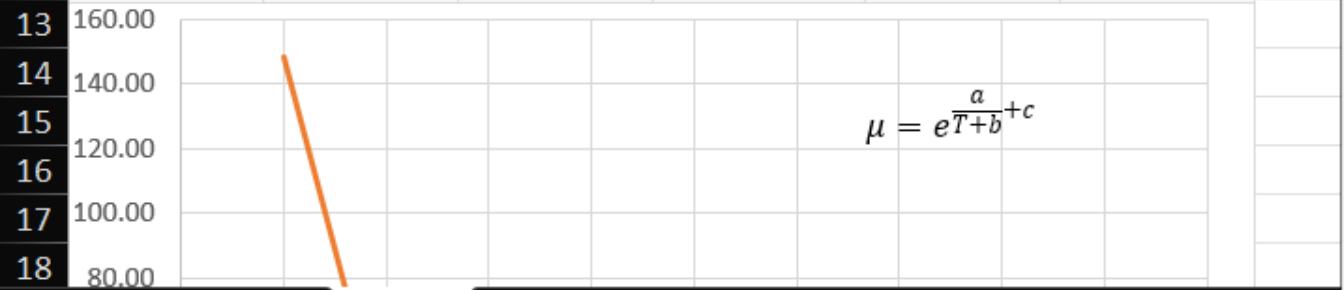
$$\mu = e^{\frac{a}{T+b}+c}$$



Obtener y transformar datos Consultas & conexiones Tipos de datos

	A	B	C	D	E	F
1	T (C°)	μ (cP)	μ(T)	Error²		
2	10	1.30	148.41	2.16E+04	a =	1.00E+02
3	20	1.00	28.03	7.31E+02	b =	1.00E+01
4	30	0.80	12.18	1.30E+02	c =	0.00E+00
5	40	0.65	7.39	4.54E+01		
6	50	0.54	5.29	2.26E+01		
7	60	0.46	4.17	1.38E+01		
8	70	0.40	3.49	9.55E+00		
9	80	0.35	3.04	7.22E+00		
10	90	0.31	2.72	5.80E+00		
11			Suma =	2.26E+04		

$$\text{Min}_{a,b,c} \sum_{i=1}^n \left(y_i - e^{\frac{a}{T_i} + b} \right)^2$$



Parámetros de Solver

Establecer objetivo: SDS11

Para: Máx Mín Valor de: 0

Cambiando las celdas de variables: SFS2:SFS4

Sujeto a las restricciones:

Convertir variables sin restricciones en no negativas

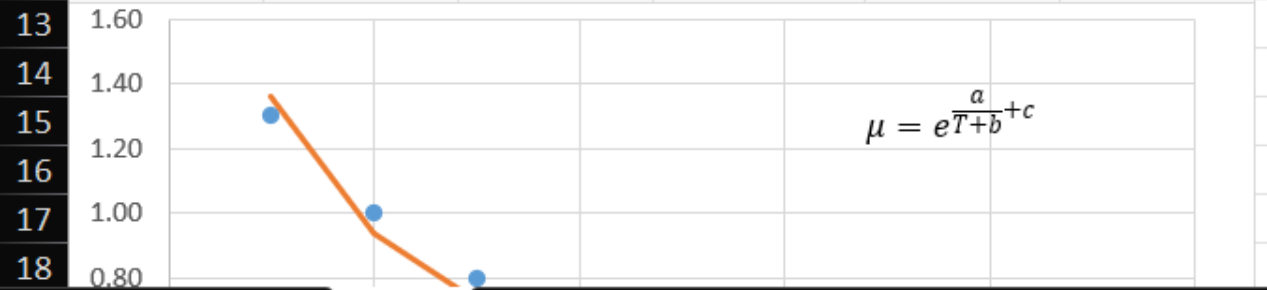
Método de resolución: GRG Nonlinear

Método de resolución: Seleccione el motor GRG Nonlinear para problemas de Solver no lineales suavizados. Seleccione el motor LP Simplex para problemas de Solver lineales, y seleccione el motor Evolutionary para problemas de Solver no suavizados.

Resolver

	A	B	C	D	E	F
1	T (C°)	μ (cP)	μ(T)	Error²		
2	10	1.30	1.36	3.77E-03	a =	8.21E+01
3	20	1.00	0.94	4.11E-03	b =	3.21E+01
4	30	0.80	0.73	5.49E-03	c =	-1.64E+00
5	40	0.65	0.60	2.10E-03		
6	50	0.54	0.53	1.98E-04		
7	60	0.46	0.47	1.39E-04		
8	70	0.40	0.43	1.04E-03		
9	80	0.35	0.40	2.74E-03		
10	90	0.31	0.38	4.75E-03		
11			Suma =	2.43E-02		

$$\text{Min}_{a,b,c} \sum_{i=1}^n y_i$$



Resultados de Solver

Solver encontró una solución. Se cumplen todas las restricciones y condiciones óptimas.

Conservar solución de Solver

Restaurar valores originales

Volver al cuadro de diálogo de parámetros de Solver

Informes de esquema

Informes

- Responder
- Sensibilidad
- Límites

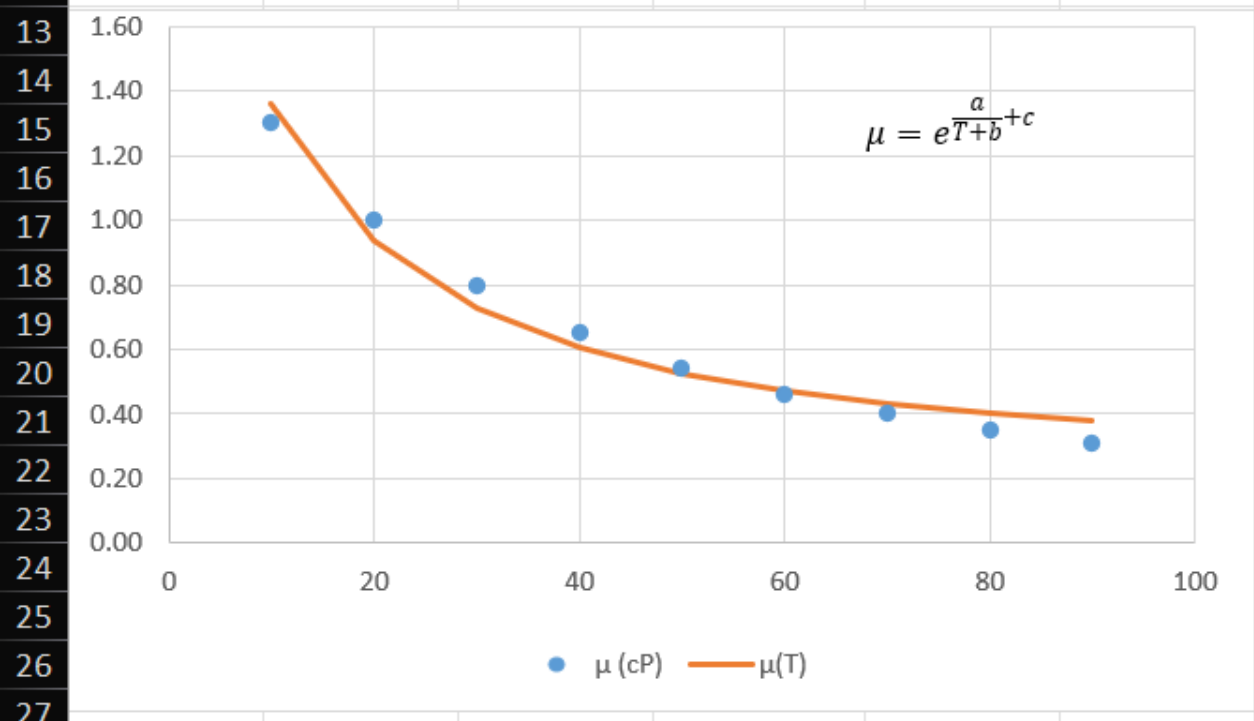
Aceptar **Cancelar** **Guardar escenario...**

Solver encontró una solución. Se cumplen todas las restricciones y condiciones óptimas.

Al usar el motor GRG, Solver ha encontrado al menos una solución óptima local. Al usar Simplex LP, significa que Solver ha encontrado una solución óptima global.

I3

	A	B	C	D	E	F	G	H	I	J	K	L
10	90	0.31	0.38	4.75E-03								
11			Suma =	2.43E-02								

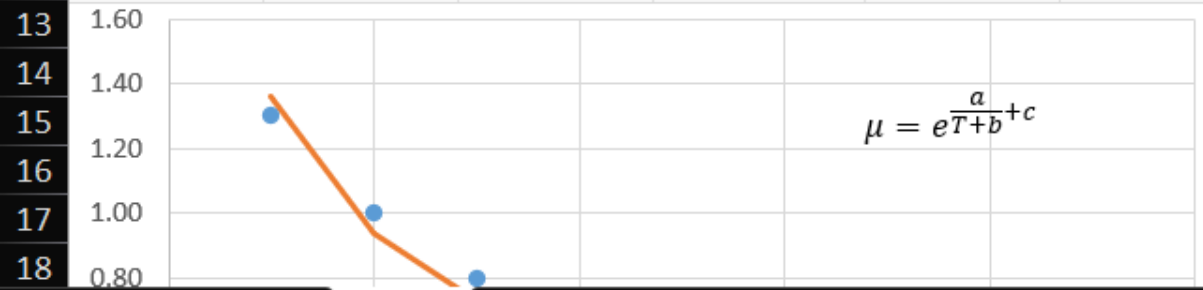


No es un buen ajuste.
Hay que ejecutar nuevamente Solver.

	A	B	C	D	E	F
1	T (C°)	μ (cP)	μ(T)	Error²		
2	10	1.30	1.36	3.77E-03		
3	20	1.00	0.94	4.11E-03		
4	30	0.80	0.73	5.49E-03		
5	40	0.65	0.60	2.10E-03		
6	50	0.54	0.53	1.98E-04		
7	60	0.46	0.47	1.39E-04		
8	70	0.40	0.43	1.04E-03		
9	80	0.35	0.40	2.74E-03		
10	90	0.31	0.38	4.75E-03		
11			Suma =	2.43E-02		

a = 8.21E+01
b = 3.21E+01
c = -1.64E+00

$$\text{Min}_{a,b,c} \sum_{i=1}^n (y_i - \mu(T_i))^2$$



Parámetros de Solver

Establecer objetivo:

Para: Máx Mín Valor de:

Cambiando las celdas de variables:

Sujeto a las restricciones:

Convertir variables sin restricciones en no negativas

Método de resolución:

Método de resolución
 Seleccione el motor GRG Nonlinear para problemas de Solver no lineales suavizados. Seleccione el motor LP Simplex para problemas de Solver lineales, y seleccione el motor Evolutionary para problemas de Solver no suavizados.

Botones: Agregar, Cambiar, Eliminar, Restablecer todo, Cargar/Guardar, Ayuda, Resolver, Cerrar

	A	B	C	D	E	F
1	T (C°)	μ (cP)	μ(T)	Error²		
2	10	1.30	1.30	5.16E-15	a =	5.78E+02
3	20	1.00	1.00	1.98E-06	b =	1.34E+02
4	30	0.80	0.80	1.32E-05	c =	-3.75E+00
5	40	0.65	0.65	4.65E-08		
6	50	0.54	0.54	7.45E-06		
7	60	0.46	0.46	2.36E-06		
8	70	0.40	0.40	1.49E-06		
9	80	0.35	0.35	4.96E-07		
10	90	0.31	0.31	1.62E-07		
11			Suma =	2.72E-05		

$$\text{Min}_{a,b,c} \sum_{i=1}^n y_i$$



Resultados de Solver

Solver ha convergido a la solución actual. Se cumplen todas las restricciones.

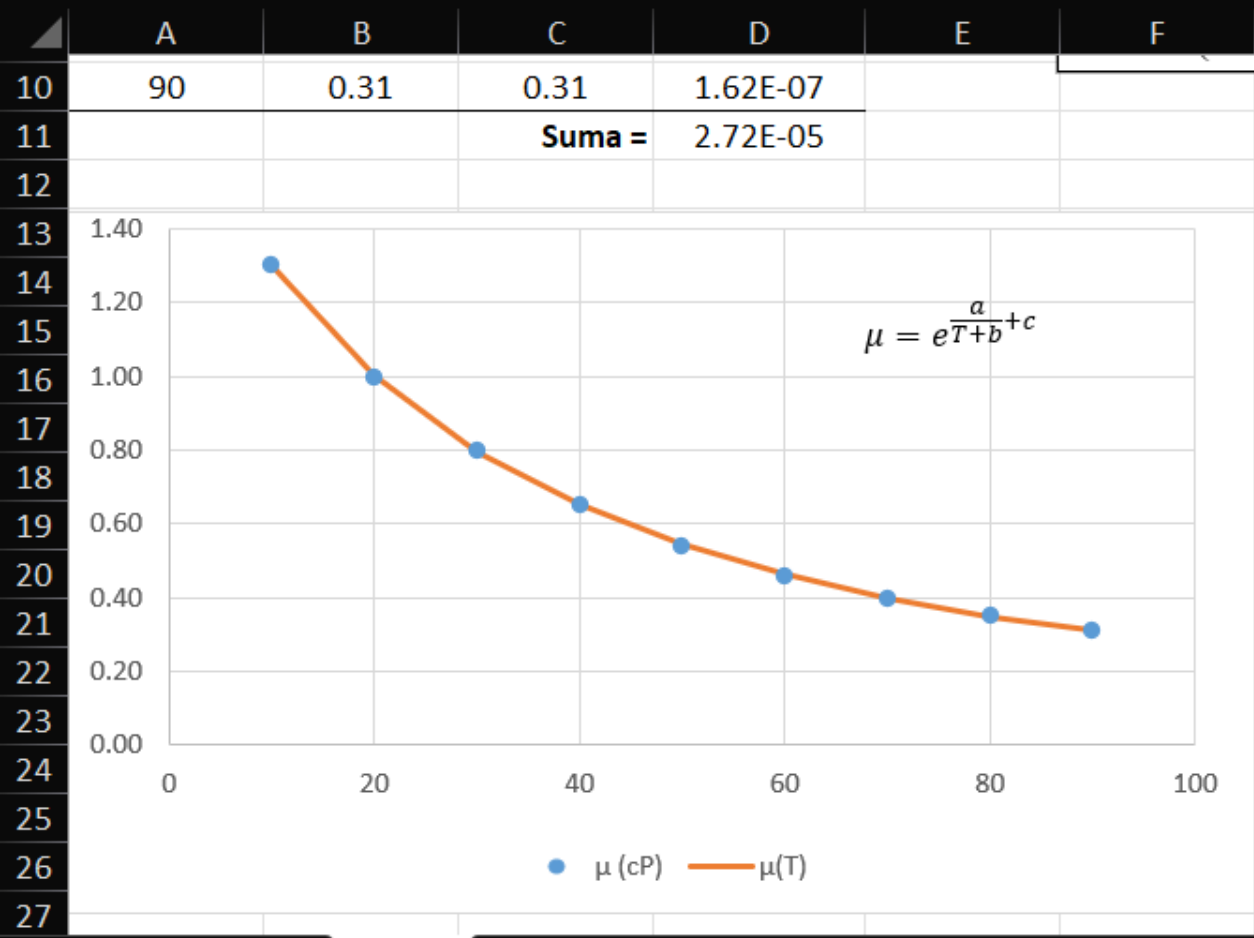
Conservar solución de Solver
 Restaurar valores originales

Volver al cuadro de diálogo de parámetros de Solver

Informes de esquema

Responder
 Sensibilidad
 Límites

Solver realizó 5 iteraciones para las que el objetivo no se movió de manera significativa. Intente usar un valor de convergencia más pequeño u otro punto de inicio.



Es un buen ajuste.
Tiene el mínimo valor de la
suma de los errores al cuadrado.

Inicio múltiple en Solver

Opciones

Todos los métodos | GRG Nonlinear | Evolutionary

Convergencia: 0.0001

Derivados

Adelantada Central

Inicio múltiple

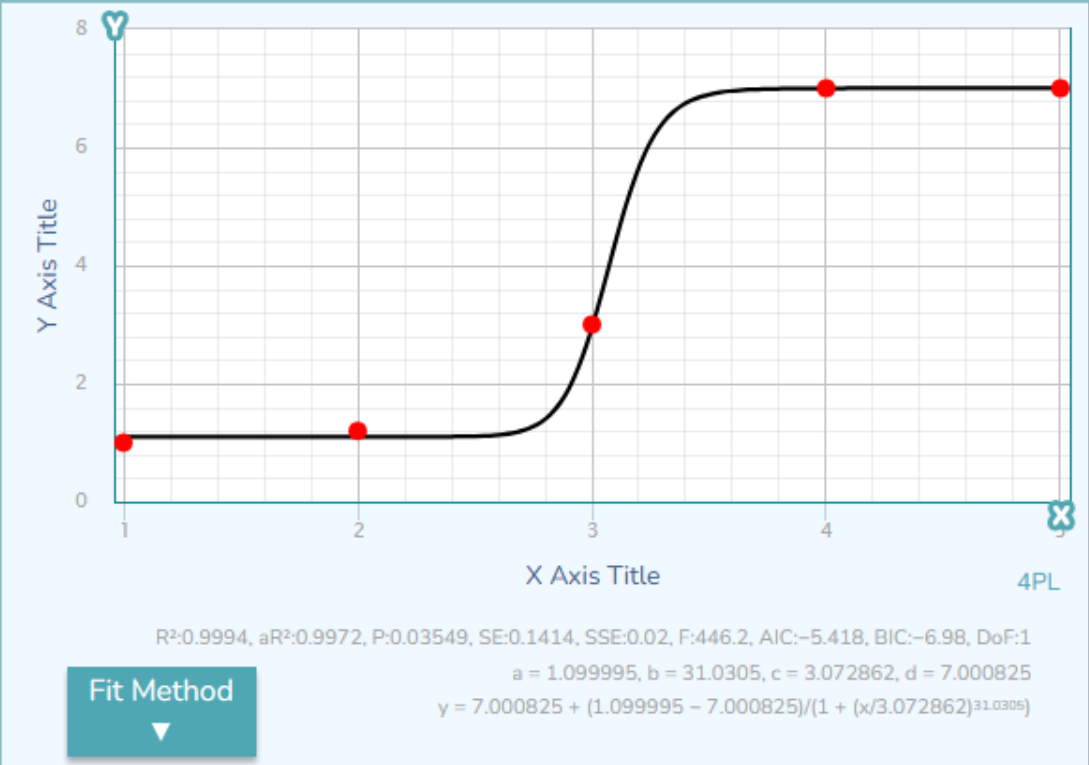
Usar inicio múltiple

Tamaño de población: 100

Valor de inicialización aleatorio: 1

Requerir límites en variables

Aceptar Cancelar



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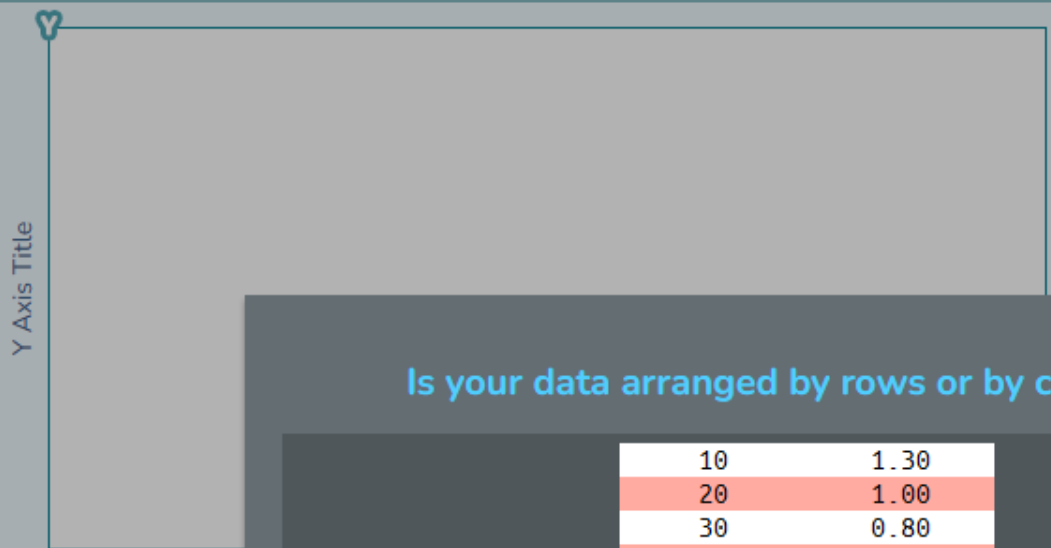
Export XLSX ▼ Share

Predict ▼

X Axis Title	Y Axis Title
1	1
2	1.2
3	3
4	7
5	7

- Swap
- Paste
- Clear

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Fit Method
▼

X Axis Title

Clear

Undo

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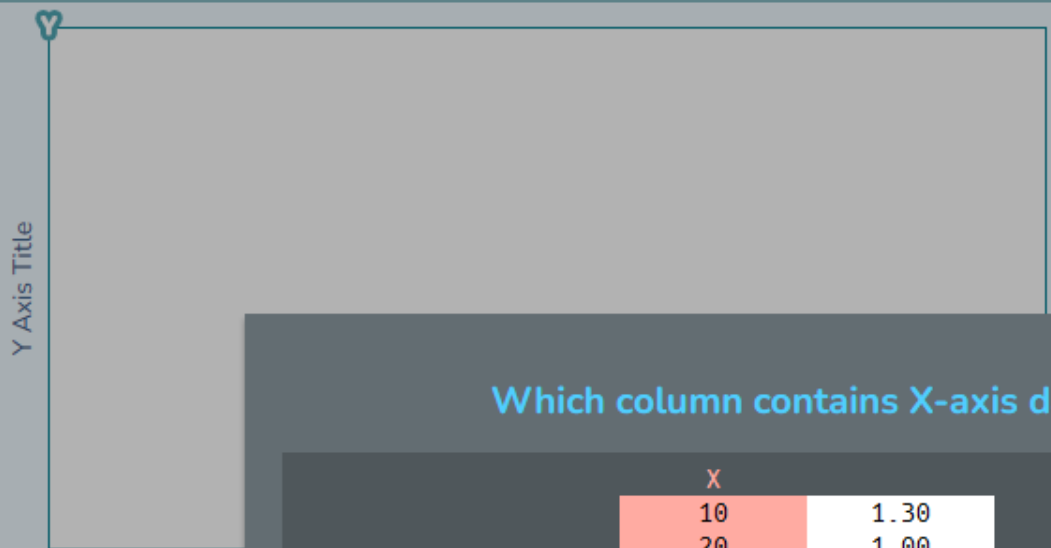
Is your data arranged by rows or by columns ?

10	1.30
20	1.00
30	0.80
40	0.65
50	0.54
60	0.46
70	0.40
80	0.35
90	0.31

- By **Row** (X and Y data on each row)
- By **Column** (X and Y data in each column)

Next

Cancel



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Fit Method
▼

X Axis Title

Input area for data entry.

Paste
Clear
Undo

Which column contains X-axis data?

X	
10	1.30
20	1.00
30	0.80
40	0.65
50	0.54
60	0.46
70	0.40
80	0.35
90	0.31

Click the **X-axis** data column

Previous Next Cancel

[How to enter my data?](#)



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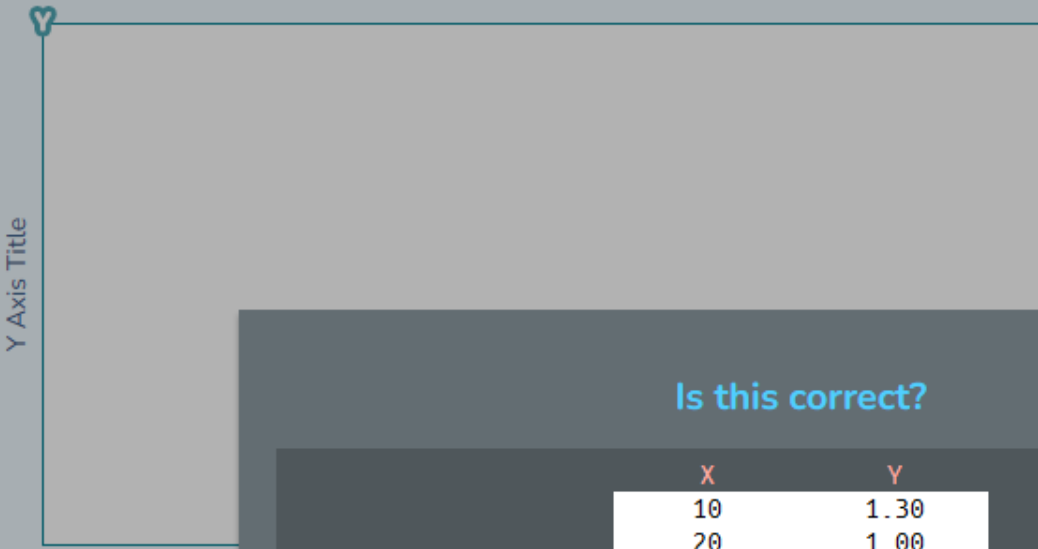
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Fit Method
▼

X Axis Title

Input area for data or fit parameters

- Paste
- Clear
- Undo

Is this correct?

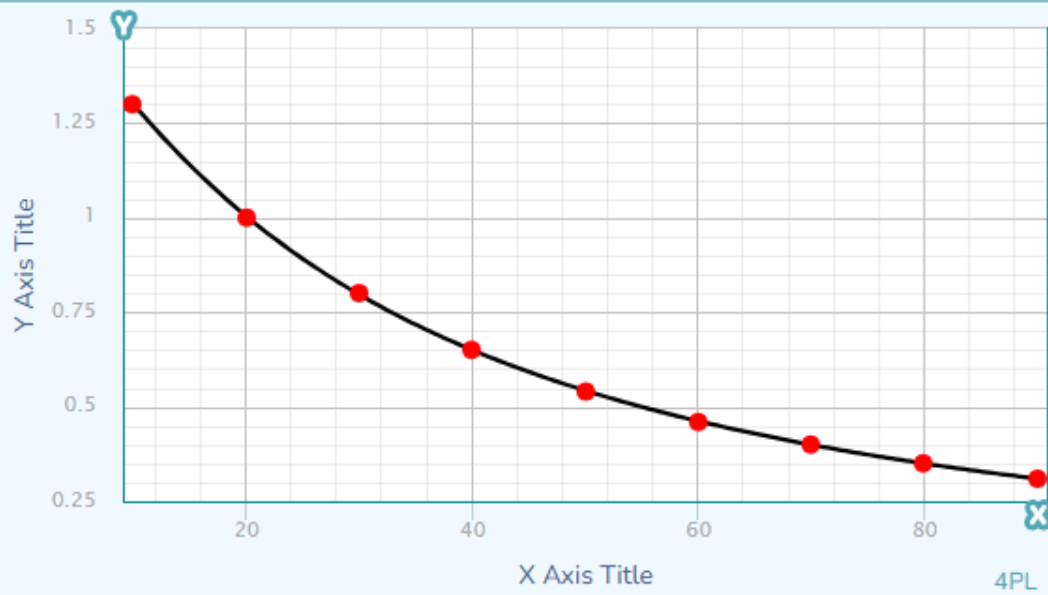
X	Y
10	1.30
20	1.00
30	0.80
40	0.65
50	0.54
60	0.46
70	0.40
80	0.35
90	0.31

Click **Apply** to accept.

Previous

Apply

Cancel



R²:1, aR²:0.9999, P:3.458*10⁻¹¹, SE:0.002646, SSE:0.00003501, F:31550, AIC:-78.57, BIC:-77.78, DoF:5, AICc:-68.57

a = 1.659682, b = 1.234282, c = 28.6026, d = -0.01846477

y = -0.01846477 + (1.659682 - -0.01846477)/(1 + (x/28.6026)^{1.234282})

Fit Method
▼

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Share

Predict ▼

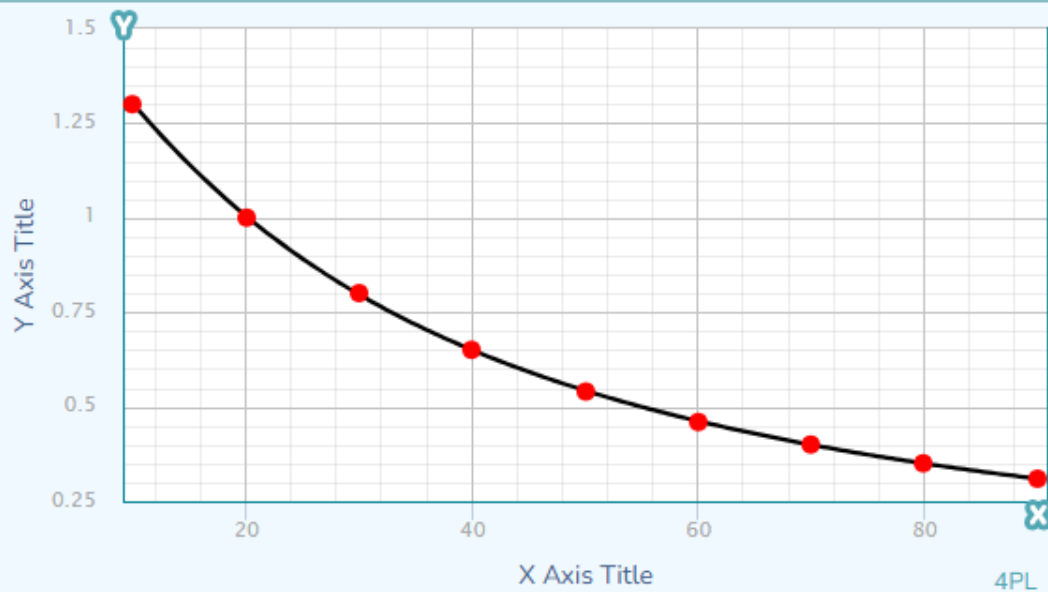
X Axis Title	Y Axis Title
10	1.3
20	1
30	0.8
40	0.65
50	0.54
60	0.46
70	0.4
80	0.35
90	0.31

Swap

Paste

Clear

Undo



R²:1, aR²:0.9999, P:3.458*10⁻¹¹, SE:0.002646, SSE:0.00003501, F:31550, AIC:-78.57, BIC:-77.78, DoF:5, AICc:-68.57

a = 1.659682, b = 1.234282, c = 28.6026, d = -0.01846477

$$y = -0.01846477 + (1.659682 - -0.01846477)/(1 + (x/28.6026)^{1.234282})$$

Fit Method ▲

- Linear ▶
- Polynomial ▶
- Nonlinear ▶
- Cubic Spline ▶
- User Defined

Weighting ▼

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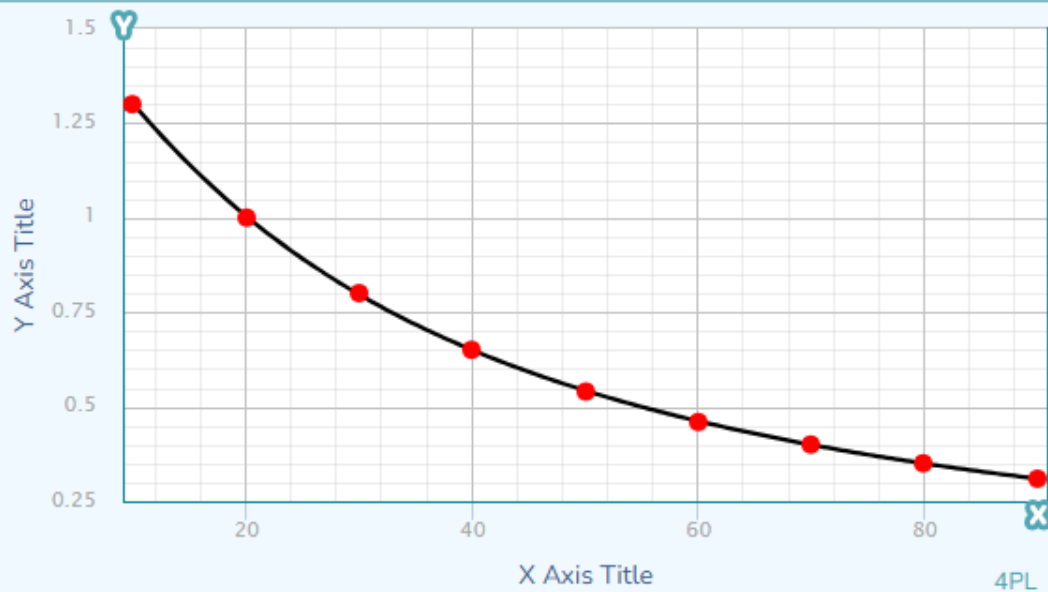
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- Set axes titles
- Try different fit methods
- Use your fit for predictions

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R²:1, aR²:0.9999, P:3.458*10⁻¹¹, SE:0.002646, SSE:0.00003501, F:31550, AIC:-78.57, BIC:-77.78, DoF:5, AICc:-68.57

a = 1.659682, b = 1.234282, c = 28.6026, d = -0.01846477

$$y = -0.01846477 + (1.659682 - -0.01846477)/(1 + (x/28.6026)^{1.234282})$$

Fit Method ▲

Linear ▶

Polynomial ▶

Nonlinear ▶

Cubic Spline ▶

User Defined

Weighting ▼

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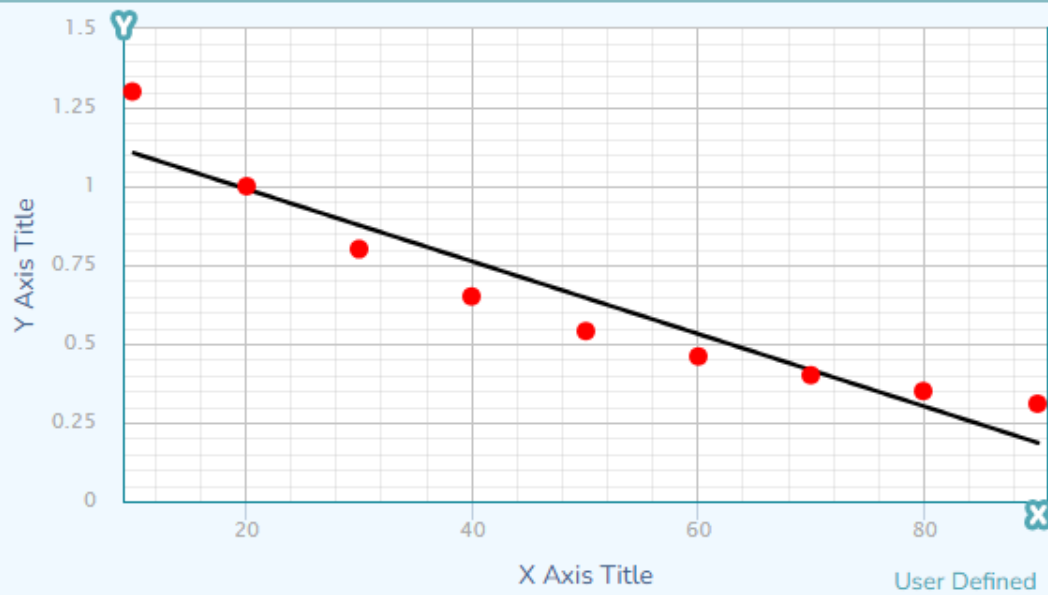
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$R^2: 0.898$, $aR^2: 0.8689$, $P: 0.0003388$, $SE: 0.1135$, $SSE: 0.09012$, $F: 30.82$, $AIC: -11.89$, $BIC: -11.5$, $DoF: 7$, $AICc: -9.893$
 $c = 1.220556$, $m = -0.0115$
 $y = -0.0115x + 1.220556$

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Fit Method



Linear ▶

Polynomial ▶

Nonlinear ▶

Cubic Spline ▶

User Defined

[How to define my fit?](#)

y=

Weighting



Initial Estimates: [What's this?](#)

Constraints: [What's this?](#)

c=

Min:

Max:

1.220556

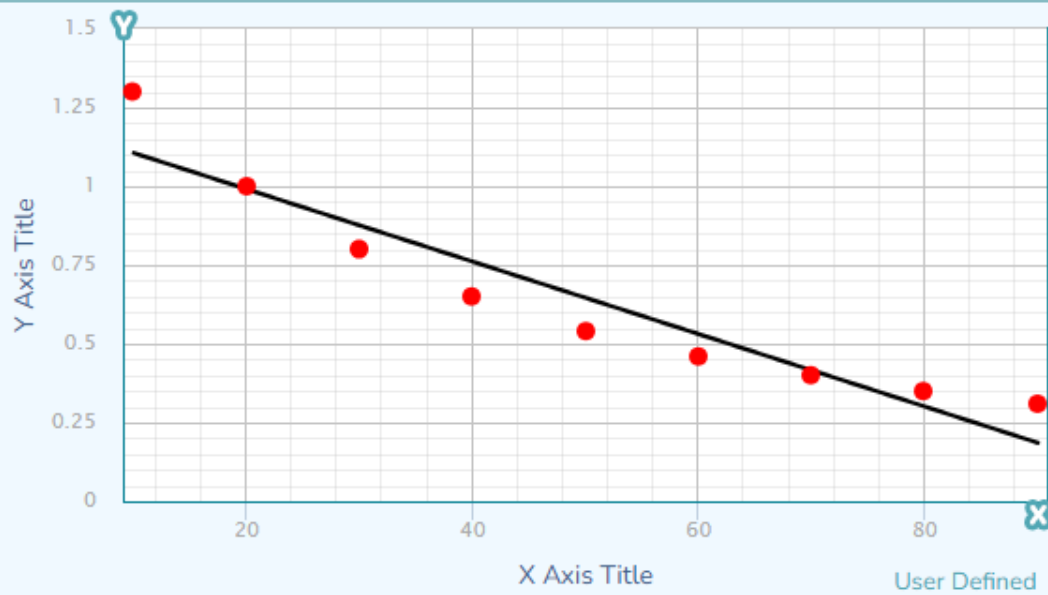
m=

Min:

Max:

-0.0115

Plot estimate



$R^2: 0.898$, $aR^2: 0.8689$, $P: 0.0003388$, $SE: 0.1135$, $SSE: 0.09012$, $F: 30.82$, $AIC: -11.89$, $BIC: -11.5$, $DoF: 7$, $AICc: -9.893$
 $c = 1.220556$, $m = -0.0115$
 $y = -0.0115x + 1.220556$

Fit Method ▲

- Linear ▶
- Polynomial ▶
- Nonlinear ▶
- Cubic Spline ▶
- User Defined

[How to define my fit?](#)

y=

Weighting ▼

Apply

Initial Estimates: [What's this?](#) Constraints: [What's this?](#)

c= Min: Max:
 m= Min: Max:

Welcome to MyCurveFit

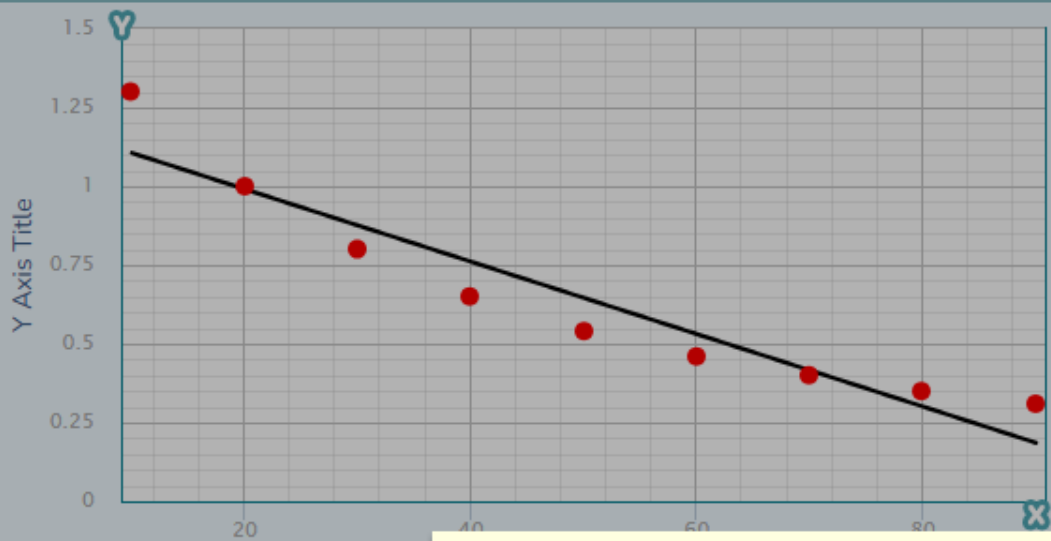
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R²:0.898, aR²:0.8689, P:0.0003388, SE:0.1135, S

To use more coefficients, please login or join. It is free to create an account and access more functionality.

Log in Join Cancel

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- Fit Method ▲
- Linear ▶
 - Polynomial ▶
 - Nonlinear ▶
 - Cubic Spline ▶
 - User Defined

y=

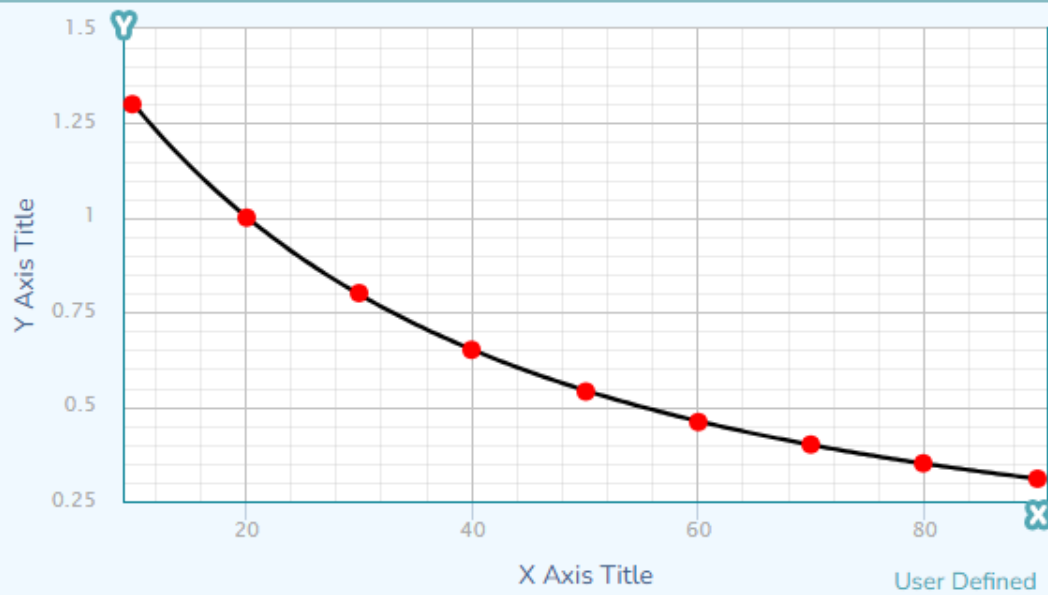
Weighting ▼

Initial Estimates: [What's this?](#) Constraints: [What's this?](#)

c= Min: Max: 1.220556

m= Min: Max: -0.0115

Plot estimate



$R^2:1$, $aR^2:1$, $P:6.384 \times 10^{-14}$, $SE:0.00213$, $SSE:0.00002721$, $F:64940$, $AIC:-82.84$, $BIC:-82.25$, $DoF:6$, $AICc:-78.04$
 $a = 577.5535$, $b = 133.8519$, $c = -3.752549$
 $y = \exp(577.5535/(x + 133.8519) - 3.752549)$

Fit Method ▲

- Linear ▶
- Polynomial ▶
- Nonlinear ▶
- Cubic Spline ▶
- User Defined

[How to define my fit?](#)

y=

Weighting ▼

Initial Estimates: [What's this?](#) Constraints: [What's this?](#)

a=	<input type="text" value="1"/>	Min:	<input type="text"/>	Max:	<input type="text"/>	577.5535
b=	<input type="text" value="1"/>	Min:	<input type="text"/>	Max:	<input type="text"/>	133.8519
c=	<input type="text" value="1"/>	Min:	<input type="text"/>	Max:	<input type="text"/>	-3.752549

Welcome to MyCurveFit

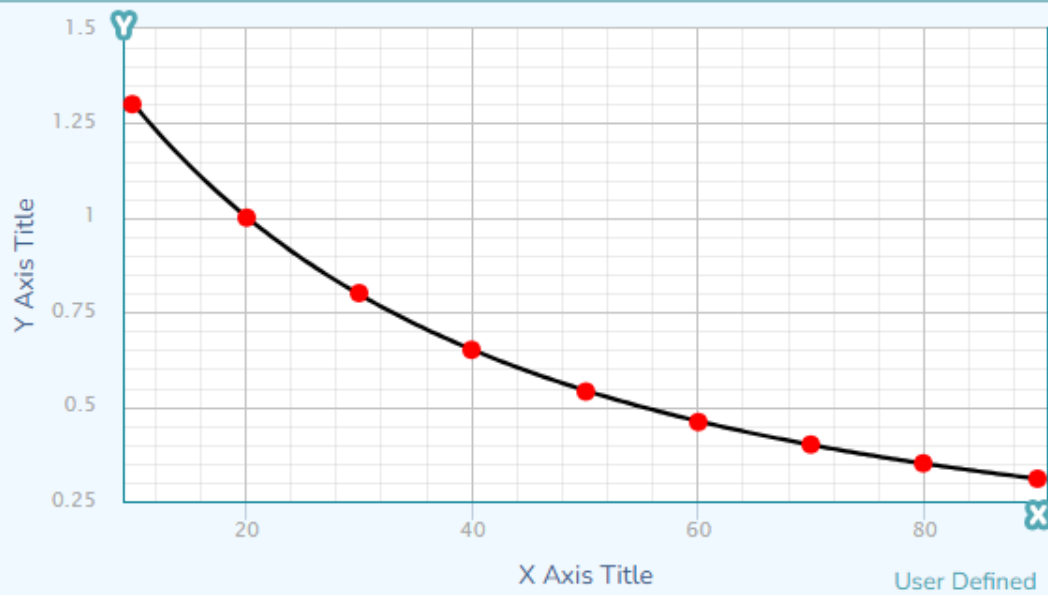
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- Set axes titles
- Try different fit methods
- Use your fit for predictions

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Goodness Measures What's this?	
R ²	1
aR ²	1
P	6.384*10 ⁻¹⁴
SE	0.00213
SSE	0.00002721
F	64940
AIC	-82.84
BIC	-82.25
DoF	6
AICc	-78.04
Coefficients	
a	577.5535 ± 23.74
b	133.8519 ± 3.439
c	-3.752549 ± 0.07005
Equation	
$y = \exp(577.5535/(x + 133.8519) - 3.752549)$	

Fit Method ▲

Linear ▶

Copy Fit Details Export Equation

[How to define my fit?](#)

Weighting ▼

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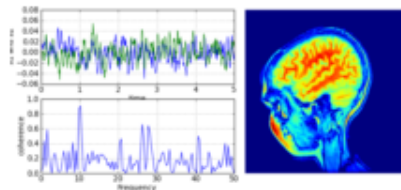
This is a mirror of ZunZun.com, which is currently offline under mysterious circumstances. Few modifications have been made, including contact information of the original author.

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If you're looking for high quality curve fitting and surface fitting, this is the site for you! Source code is available at the [Bitbucket Code Repository](#).

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Introduction

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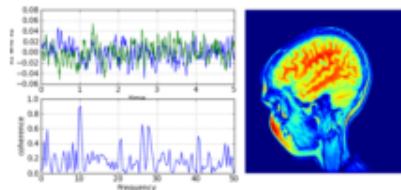
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2D User Defined Function

[User Defined Function 2D](#) $y = \text{user defined function}$

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- Introduction
- Text Data Editor**
- User Defined Function Editor
- Fitting Target
- Data Labels For Graphs
- Graph Scaling And Lin/Log Control
- Graph Size
- Scientific Notation For Graphs

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Pulldown Menu

Text Data Editor ▼

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Text data editor

Cut-and-paste text or edit data here

- Convert commas to spaces (1,2,0,3 yields 1 2 0 3)
- Use comma as decimal separator (1,203 = 1.203)
- Remove commas from text (1,2,0,3 yields 1203)

- Standard Unweighted Fitting: no weights required
- Weighted Fitting: each data point requires a weight

This data is provided as an example, cut and paste as needed to model your data. All lines of text that do not begin with a number are ignored.

Weighted fitting requires an additional number to be used as a weight when fitting. The site does not calculate any weights, which are used as:
$$\text{error} = \text{weight} * (\text{predicted} - \text{actual})$$
You must provide any weights you wish to use.

X	Y
5.357	0.376
5.457	0.489
5.797	0.874

Clear All Text

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Text data editor

Cut-and-paste text or edit data here

- Convert commas to spaces (1,2,0,3 yields 1 2 0 3)
- Use comma as decimal separator (1,203 = 1.203)
- Remove commas from text (1,2,0,3 yields 1203)

- Standard Unweighted Fitting: no weights required
- Weighted Fitting: each data point requires a weight

X	Y
10	1.30
20	1.00
30	0.80
40	0.65
50	0.54
60	0.46
70	0.40
80	0.35
90	0.31

Clear All Text



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Graph Size

Scientific Notation For Graphs

Text data editor

Enter text or edit data here

Separates data into spaces (1,2,0,3 yields 1 2 0 3)

Specifies decimal separator (1,203 = 1.203)

Removes spaces from text (1,2,0,3 yields 1203)

- Standard Unweighted Fitting: no weights required
- Weighted Fitting: each data point requires a weight

X	Y
10	1.30
20	1.00
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Clear All Text

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User Defined Function Editor

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Text Function Editor

Cut-and-paste text or edit your function here

```
# Enter the text of your function here. Comments begin
# with a "#". Lines with no text are ignored.
# Use an upper case "X" to represent your data.
# Note that most spreadsheets use log base 10 for
# a LOG() function, here log() is the natural log.
# The site uses power() or **, not the caret '^'.
# The site uses fabs() not abs() for absolute value.
# The web site will automatically decode the
# parameter names (coefficient names) that you use.
# See the examples below for ideas on function entry.
```

Example User Defined Functions

```
C * exp(2.2/X) + 51.0 + pi ** e - sinc(1.1) / [B + A] # coefficients are A, B and C
```

```
Scale * exp(X) + offset # Scale and offset are coefficients in this example
```

```
# the following three examples are equivalent
power(X+shift, C0) # shift and C0 are coefficients in this example
[X+shift] ** C0    # shift and C0 are coefficients in this example
(X+shift) ** C0    # shift and C0 are coefficients in this example
```

```
MX + B # This fails, it should be written as M*X + B
```

Links To Help For Pre-Defined Internal Functions

Exponents And Logarithms: [exp](#) [log](#) [log10](#) [log2](#)

Pulldown Menu

User Defined Function Editor ▼

Submit (may take several minutes)

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Text Function Editor

Cut-and-paste text or edit your function here

```
exp(a/(X+b)+c)
```

Example User Defined Functions

```
C * exp(2.2/X) + 51.0 + pi ** e - sinc(1.1) / [B + A] # coefficients are A, B and C
```

```
Scale * exp(X) + offset # Scale and offset are coefficients in this example
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```
# the following three examples are equivalent  
power(X+shift, C0) # shift and C0 are coefficients in this example  
[X+shift] ** C0    # shift and C0 are coefficients in this example  
(X+shift) ** C0   # shift and C0 are coefficients in this example
```

```
MX + B # This fails, it should be written as M*X + B
```

Links To Help For Pre-Defined Internal Functions

Exponents And Logarithms: [exp](#) [log](#) [log10](#) [log2](#)

Fitting Data

Elapsed time: 00:00:00 (hh:mm:ss)

Current time on server: Fri Jun 12 17:55:23

Time of last update : Fri Jun 12 17:55:23

Server load average for the past 1 minute: 0.06

Server load average for the past 5 minutes: 0.12

Server load average for the past 15 minutes: 0.16

Load < 2 means the server cores are running with a light load.

Load = 2 means the server cores each average 100% CPU with a single user.

Load > 2 means the server cores each average 100% CPU with multiple users.

Coefficients And Text Reports

Histograms

Statistical Scatterplots

Data Graphs

Introduction and PDF Link ▼

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Introduction and PDF Link

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[tkinter](#) [pyQt5](#) [pyGtk](#) [wxPython](#)

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[Animated Confidence Intervals](#)
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Core fitting library source code
[pyeq2 \(Python 2\)](#) [pyeq3](#)

[Link to additional information and history](#)

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- Introduction and PDF Link ▾
- Introduction and PDF Link
- Evaluate This Equation At A Point
- User Defined Function Text
- Coefficients**
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- Error Statistics
- Data Statistics

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Coefficients And Text Reports

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▾

▾

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Coefficients

y = User Defined Function

Fitting target of lowest sum of squared absolute error = 2.7210617700971931E-05

a = 5.7755349118308777E+02

b = 1.3385187426769699E+02

c = -3.7525493273039130E+00

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[Django \(this site\)](#) [Django \(Python 2\)](#) [Flask](#) [CherryPy](#) [Bottle](#)

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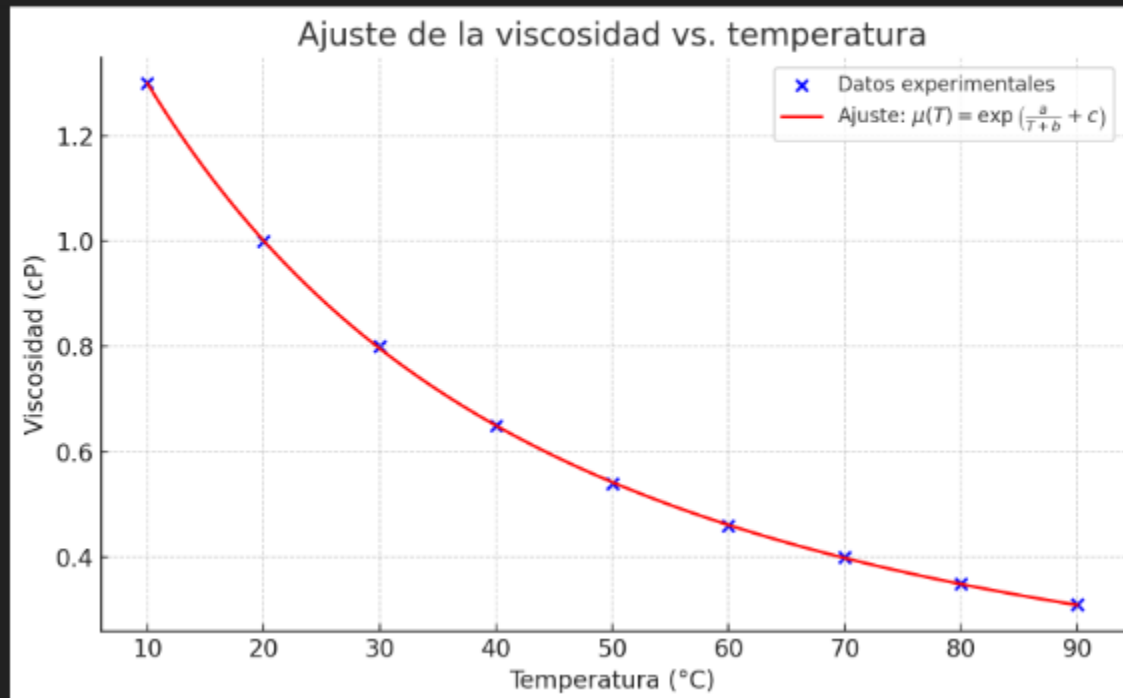
Prompt para regresión

Con los datos de la tabla que te envió, de viscosidad μ en función de la temperatura T , ajusta por regresión los coeficientes de la siguiente función: $\mu(T) = \exp(a/(T+b)+c)$.

10	1.30
20	1.00
30	0.80
40	0.65
50	0.54
60	0.46
70	0.40
80	0.35
90	0.31

Con los datos de la tabla que te envió, de viscosidad μ en función de la temperatura T , ajusta por regresión los coeficientes de la siguiente función: $\mu(T) = \exp(a/(T+b)+c)$.

Ajuste De La Viscosidad Vs. Temperatura



Claro, expresando los coeficientes ajustados con **cuatro cifras significativas**, tenemos:

$$\mu(T) = \exp\left(\frac{a}{T+b} + c\right)$$

Con:

- $a = 577.6$
- $b = 133.9$
- $c = -3.753$

Entonces, la ecuación ajustada queda:

$$\mu(T) = \exp\left(\frac{577.6}{T+133.9} - 3.753\right)$$

✦ *Importante:* esta fórmula está en función de la **temperatura T en grados Celsius** y da la viscosidad μ en **centipoise (cP)**.



Temperaturas de la correlación

En °C

En K

- $a = 577.6$
- $b = 133.9$
- $c = -3.753$

- $a = 577.6$
- $b = 133.9 - 273.15 = -139.25$
- $c = -3.753$

- En correlaciones y expresiones donde la temperatura figura sola, se suele trabajar con temperaturas absolutas.
- En correlaciones y expresiones donde la presión figura sola, se suele trabajar con presión absoluta.

Mapa curricular de programación no lineal

1. Operación con ciclos
2. Criterio técnico
3. Función objetivo
4. Restricciones
5. Parámetros
6. Variables de decisión
7. Regresión
8. Resolución con LINGO y Excel