

$$T(n) = \begin{cases} 1, & n = 1 \\ 3T(n-1) + (1/n) & n > 1 \end{cases}$$

$$T(n) = 3T(n-1) + \left(\frac{1}{n}\right) \quad k = 1$$

$$T(n) = 3 \left[3T(n-1-1) + \left(\frac{1}{n-1}\right) \right] + \left(\frac{1}{n}\right) = 9T(n-2) + 3 \left(\frac{1}{n-1}\right) + \left(\frac{1}{n}\right) \quad k = 2$$

$$\begin{aligned} T(n) &= 9 \left[3T(n-2-1) + \left(\frac{1}{n-2}\right) \right] + 3 \left(\frac{1}{n-1}\right) + \left(\frac{1}{n}\right) = \\ &= 27T(n-3) + 9 \left(\frac{1}{n-2}\right) + 3 \left(\frac{1}{n-1}\right) + \left(\frac{1}{n}\right) \quad k = 3 \end{aligned}$$

$$\begin{aligned} T(n) &= 27 \left[3T(n-3-1) + \left(\frac{1}{n-3}\right) \right] + 9 \left(\frac{1}{n-2}\right) + 3 \left(\frac{1}{n-1}\right) + \left(\frac{1}{n}\right) = \\ &= 81T(n-4) + 27 \left(\frac{1}{n-3}\right) + 9 \left(\frac{1}{n-2}\right) + 3 \left(\frac{1}{n-1}\right) + \left(\frac{1}{n}\right) \quad k = 4 \end{aligned}$$

$$T(n) = 3^k \cdot T(n-k) + \sum_{i=0}^{k-1} 3^i \left(\frac{1}{n-i}\right)$$

como $T(1) = 1 \Rightarrow n - k = 1 \Rightarrow k = n - 1$

$$T(n) = 3^{n-1} \cdot T(n - (n-1)) + \sum_{i=0}^{n-2} 3^i \left(\frac{1}{n-i}\right)$$

$$T(n) = 3^{n-1} + \sum_{i=0}^{n-2} 3^i \left(\frac{1}{n-i}\right)$$

$$\emptyset \in (3^n)$$